

**AMENDMENTS TO THE CLAIMS:**

This listing of claims will replace all prior versions, and listings, of claims in the application:

**LISTING OF CLAIMS:**

1. (Currently Amended) A cryptographic method in an electronic component during which a modular exponentiation of the type  $x^d$  is performed, with  $d$  an integer exponent of  $m+1$  bits, by scanning the bits of  $d$  from left to right in a loop indexed by  $i$  varying from  $m$  to 0 and calculating and storing in an accumulator ( $R0$ ), at each turn of rank  $i$ , an updated partial result equal to  $x^b(i)$ ,  $b(i)$  being the  $m-i+1$  most significant bits of the exponent  $d$  ( $b(i) = d_{m-i}$ ), ~~the method being characterised in that wherein~~, at the end of a turn of rank  $i(j)$  ( $i = i(0)$ ) chosen randomly, a randomisation step E1 is performed during which:

E1: a random number  $z$  ( $z = b(i(j))$ ,  $z = b(i(j)).2^t$ ,  $z = u$ ) is subtracted from a part of the bits of  $d$  not yet used ( $d_{i-1>0}$ ) in the method

then, after having used the bits of  $d$  modified by the randomisation step E1, a consolidation step E2 is performed during which:

E2: the result of the multiplication of the content of the accumulator ( $x^b(i)$ ) by a number that is a function of  $x^z$  stored in a register ( $R1$ ) is stored ( $R0 \leftarrow R1 \times R0$ ) in the accumulator ( $R0$ ).

2. (Currently Amended) Method according to ~~the preceding claim~~ claim 1, in which step E1 is repeated one or more times, at the end of various turns of rank  $i(j)$  ( $i = i(0)$ ,  $i = i(1)$ , ...) chosen randomly between 0 and  $m$ .

3. (Currently Amended) Method according to ~~the preceding claim~~ claim 2, in which, at each turn  $i$ , it is decided randomly ( $p=1$ ) whether or not step E1 is performed.

4. (Currently Amended) A cryptographic method according to ~~one of claims 1 to 3~~ claim 1, in which the number  $z$  ( $z=b(i(j))$ ,  $z = b(i(j)).2^t$ ) is a function of the exponent  $d$ , in which, during the randomisation step, the result of the multiplication of the content of the accumulator ( $x^b(i)$ ) by the content of the register ( $R1$ ) is also stored ( $R1 \leftarrow R0 \times R1$ ) in the said register ( $R1$ ).

5. (Original) A method according to claim 4, in which the consolidation step E2 is performed after the last turn of rank  $i$  equal to 0.

6. (Currently Amended) A method according to ~~the preceding claim~~ claim 5, during which, during step E1, the number  $b(i)$  is subtracted from  $d$ .

7. (Original) A method according to claim 6, during which the following is effected:

Input:  $x, d = (d_m, \dots, d_0)_2$

Output:  $y = x^d \bmod N$

$R0 \leftarrow 1; R1 \leftarrow 1; R2 \leftarrow x, i \leftarrow m$

as long as  $i \geq 0$ , do:

$R0 \leftarrow R0 \times R0 \bmod N$

if  $d_i = 1$  then  $R0 \leftarrow R0 \times R2 \bmod N$

$p \leftarrow R\{0, 1\}$

if  $((p = 1) \text{ and } d_{i-1 \rightarrow 0} \geq d_{m \rightarrow i})$  then

$d \leftarrow d - d_{m \rightarrow i}$

$R1 \leftarrow R1 \times R0 \bmod N$

end if

$i \leftarrow i-1$

end as long as

$R0 \leftarrow R0 \times R1 \bmod N$

return  $R0$

8. (Currently Amended) A method according to claim 5, during which step E1 is modified as follows:

E1: a number equal to  $g \cdot b(i)$  is subtracted from  $d$ ,  $g$  being a positive integer; the current partial result ( $x^b(i)$ ) is raised to the power of  $g$  and the result is stored in the register (R1).

9. (Currently Amended) A method according to ~~the preceding claim~~ claim 8, in which  $g$  is equal to  $2^\tau$ ,  $\tau$  being a random number chosen between 0 and  $T$ .

10. (Currently Amended) A method according to ~~the preceding claim~~ claim 9, in which the following is effected:

Input:  $x, d = (d_m, \dots, d_0)_2$

Output:  $y = x^d \bmod N$

$R0 \leftarrow 1; R1 \leftarrow 1; R2 \leftarrow x, i \leftarrow m$

as long as  $i \geq 0$ , do:

$R0 \leftarrow R0 \times R0 \bmod N$

if  $d_i = 1$  then  $R0 \leftarrow R0 \times R2 \bmod N$

$\rho \leftarrow R\{0, 1\}; \tau \leftarrow R\{0, \dots, T\}$

if  $((\rho = 1) \text{ and } (d_{i-1 \rightarrow \tau} \geq d_{m \rightarrow i}))$  then

$d_{i-1 \rightarrow \tau} \leftarrow d_{i-1 \rightarrow \tau} - d_{m \rightarrow i}$

$R3 \leftarrow R0$

as long as  $(\tau > 0)$  do:

$R3 \leftarrow R3^2 \bmod N; \tau \leftarrow \tau - 1$

end as long as

$R1 \leftarrow R1 \times R3 \bmod N$

end if

$i \leftarrow i - 1$

end as long as

$R0 \leftarrow R0 \times R1 \bmod N$

return  $R0$

11. (Currently Amended) A method according to ~~one of claims 1 to 4~~ claim 1, in which the consolidation step E2 is performed at the end of the rank using the last bit of  $d$  modified during step E1.

12. (Original) A method according to claim 11, in the course of which, during step E1, the number  $b(i)$  is subtracted from the bits of  $d$  of rank  $i(j) - c(j)$  to  $i(j)-1$ ,  $c(j)$  being an integer, and the content of the accumulator ( $x^b(i(j))$ ) is stored in the register (R1).

13. (Currently Amended) A method according to ~~the preceding claim~~ claim 12, in the course of which, during the turn of rank  $i(j+1)$ , it is chosen randomly to perform step E1 only if  $i(j+1) \leq i(j) - c(j)$ . ( ~~$\epsilon = 1$  free semaphore~~).

14. (Currently Amended) A method according to claim 12 or 13, in which  $c(j)$  is equal to  $m - i(j) + 1$ .

15. (Currently Amended) A method according to ~~the preceding claim~~ claim 14, during which the following steps are performed:

Input:  $x, d = (d_m, \dots, d_0)_2$

Output:  $y = x^d \bmod N$

$R0 \leftarrow 1; R1 \leftarrow 1; R2 \leftarrow x,$

$i \leftarrow m; c \leftarrow -1; \sigma \leftarrow 1$

as long as  $i \geq 0$ , do:

$R0 \leftarrow R0 \times R0 \bmod N$

if  $d_i = 1$  then  $R0 \leftarrow R0 \times R2 \bmod N$  end if

if  $(2i \geq m+1) \text{ and } (\sigma=1)$  then  $c \leftarrow m-i+1$

if not  $\sigma = 0$

end if

$p \leftarrow R\{0, 1\}$

$\varepsilon \leftarrow p \text{ and } (d_{i-1 \rightarrow i-c} \geq d_{m \rightarrow i}) \text{ and } \sigma$

if  $\varepsilon = 1$  then

$R1 \leftarrow R0; \sigma \leftarrow 0$

$d_{i-1 \rightarrow i-c} \leftarrow d_{i-1 \rightarrow i-c} - d_{m \rightarrow i}$

end if

if  $c = 0$  then

$R0 \leftarrow R0 \times R1 \bmod N; \sigma \leftarrow 1$

end if

$c \leftarrow c-1; i \leftarrow i-1$

end as long as

return  $R0$

16. (Currently Amended) A method according to claim 12 or 13, in which  $c(j)$  is chosen randomly between  $i(j)$  and  $m-i(j)+1$ .

17. (Currently Amended) A method according to ~~the preceding claim~~ claim 16, during which the following is effected:

Input:  $x, d = (d_m, \dots, d_0)_2$

Output:  $y = x^d \bmod N$

$R0 \leftarrow 1; R1 \leftarrow 1; R2 \leftarrow x,$

$i \leftarrow m; c \leftarrow -1; \sigma \leftarrow 1$

as long as  $i \geq 0$ , do:

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R0 <- R0xR0 mod N
if  $d_i = 1$  then R0 <- R0xR2 mod N
    if  $(2i \geq m+1)$  and ( $\sigma = 1$ )
        then  $c <- R\{m-i+1, \dots, i\}$ 
        if not  $\sigma = 0$ 
             $\varepsilon <- \rho$  and  $(d_{i-1 \rightarrow i-c} \geq d_{m \rightarrow i})$  and  $\sigma$ 
            if  $\varepsilon = 1$  then
                R1 <- R0;  $\sigma <- 0$ 
                 $d_{i-1 \rightarrow i-c} <- d_{i-1 \rightarrow i-c} - d_{m \rightarrow i}$ 
            end if
            if  $c = 0$  then
                R0 <- R0xR1 mod N;  $\sigma <- 1$ 
            end if
             $c <- c-1$ ;  $i <- i-1$ 
        end as long as
    return R0

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18. (Currently Amended) A method according to ~~one of claims 1 to 2~~ claim 1, in which the number  $z$  is a number  $u$  ( $z = u$ ) of  $v$  bits chosen randomly and independent of the exponent  $d$ .

19. (Currently Amended) A method according to ~~the preceding claim~~ claim 18, in which, during step E1, the number  $u$  is subtracted from a packet  $w$  of  $v$  bits of  $d$ .

20. (Currently Amended) A method according to ~~the preceding claim~~ claim 19, during which:

- if  $H(w-u) + 1 < H(w)$ , it is chosen to perform a randomisation step E1,
- if  $H(w-u) + 1 > H(w)$ , it is chosen not to perform step E1,
- if  $H(w-1) + 1 = H(w)$ , it is chosen randomly to perform or not a randomisation step E1.

21. (Currently Amended) A method according to ~~the preceding claim~~ claim 20, during which the following is effected:

Input:  $x, d = (d_m, \dots, d_0)_2$

Parameters:  $v, k$

Output:  $y = x^d \bmod N$

$R0 \leftarrow 1; R2 \leftarrow x; i \leftarrow m; L = \emptyset$

as long as  $i \geq 0$ , do:

$R0 \leftarrow R0 \times R0 \bmod N$

if  $d_i = 1$  then  $R0 \leftarrow R0 \times R2 \bmod N$  end if

if  $i = m \bmod ((m+1)/k)$  then  $\sigma \leftarrow -1$  end if

if  $\sigma = 1$  and  $L = \emptyset$  then

$s \leftarrow 0; u \leftarrow R \{0, \dots, 2^v - 1\};$

$R1 = x^u \bmod N$

end if

$w \leftarrow d_{i-v+1}$

$h \leftarrow H(w)$

if  $w \geq u$  then  $\Delta \leftarrow w - u; h_\Delta \leftarrow 1 + H(\Delta)$

if not  $h_\Delta \leq v+2$

end if

$\rho \leftarrow R\{0, 1\}$

if  $[(\sigma=0) \wedge (i-v+1 \geq 0)] \wedge$

$[(h > h_\Delta) \text{ or } ((\rho=1) \text{ and } (h=h_\Delta))]$  then

$d_{i-v+1} \leftarrow \Delta; L \leftarrow L \cup \{i-v+1\}$

end if

if  $(i \in L)$  then

$R0 \leftarrow R0 \times R1 \bmod N$

$L \leftarrow L \setminus \{i\}$

end if

$i \leftarrow i-1$

end as long as

return  $R0$